Investigating students' difficulties with differential equations in physics

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MS225 – Introduction to Differential Equations

- Service taught to physics students and prospective mathematics teachers.
- Methods course that teaches students to solve various first and second order ODEs.
- Designed to allow students bring their expertise back to their subjects.
- 2+1 structure.
- 80% final exam.

Research Questions

1-What is the precise nature of difficulties physics students encounter in their study of differential equations?

• Aim 1: Identify the difficulties.

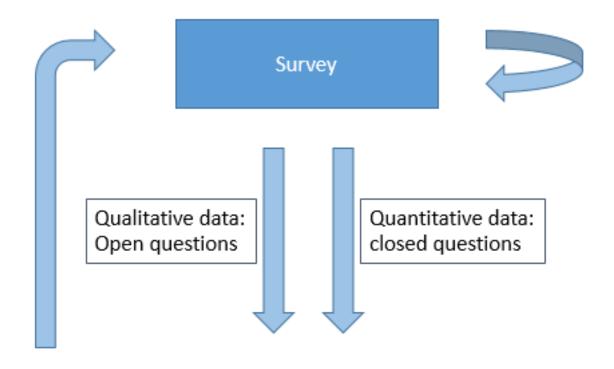
2-How best can these issues be addressed?

- Aim 2: Develop an intervention (set of tutorials) that counteract the issues.
- Aim 3: Evaluate and improve the intervention.



Research Methodology

Design Diagram

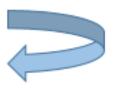


Survey containing closed and open ended questions identifies difficulties (**Aim 1**) and informs the development of an intervention (**Aim 2**).

These tutorials are trialled and improved upon using pre- post-tests and interviews (Aim 3).

The survey is also improved as the difficulties become known and the interventions can be assessed.

Intervention



Qualitative data: interviews Quantitative data: pre- post-tests

Q1. Find x and y if



Results



- Prior mathematical learning
- Conceptual issues in the study of DEs
- Transfer
- Modelling



- Survey 2.0
 - Additional questions
 - · Survey 1 vs 2



- Pre- Post-testing
- Interviews



Q2. What are differential equations, and why are they useful?

$$\frac{dT(t)}{dt} = -k(T(t) - T_0) = -kT(t) + kT_0$$

$$\frac{\mathrm{d}T(t)}{\mathrm{d}t} = -\mathrm{k}(T(t) - \mathrm{T}_0) = -\underline{\mathrm{k}}T(t) + \mathrm{k}\mathrm{T}_0 \qquad \mathbf{g} \qquad \frac{\mathrm{d}v(t)}{\mathrm{d}t} = \mathrm{g} - \mathrm{c}v(t) = -c(v(t) - \frac{\mathrm{g}}{c})$$

$$\int \frac{1}{A+Bx} dx$$

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Module information

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2014-2015 vs 2015-2016

- Content: foster conceptual understanding of DEs and the application of DEs to a physics environment in addition to procedural competence
- Methodology: encourage cooperative learning and students constructing their own knowledge through discussion in addition to allowing time to for individuals to practice the various solution techniques

APOS Theory

- Action Process Object Schema.
- Constructivist
- A theory of how mathematical concepts can be learned
- Genetic decomposition?

 $f(x) = 2x^2 + 3x - 1.$

actions processes coordination reversal de-encapsulation

Schema



Thanks for your time. Questions?