



Mirostław Brozis

IBL in maths lesson

- is it possible?

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WHY ?

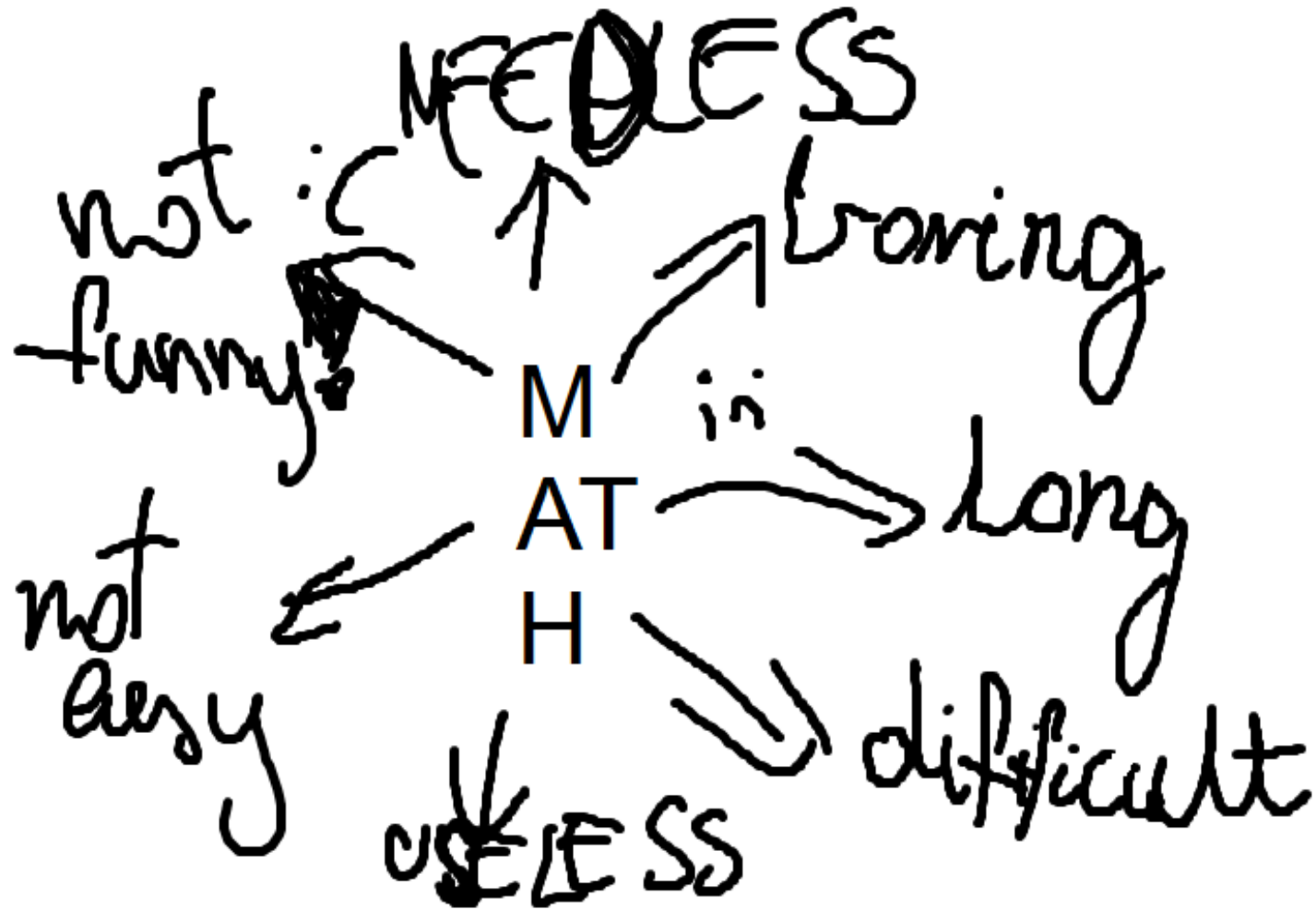
HOW ? - case study

WHERE ?

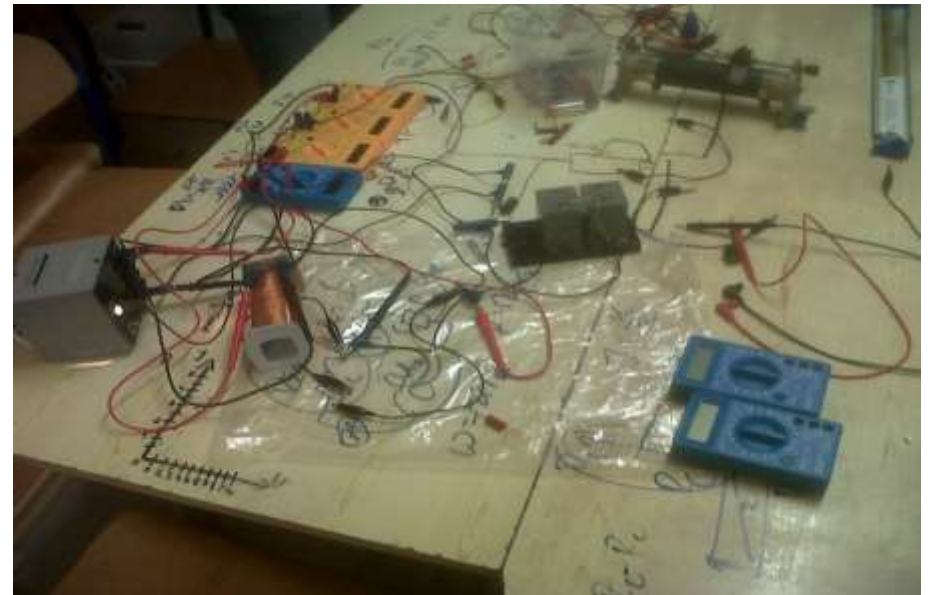
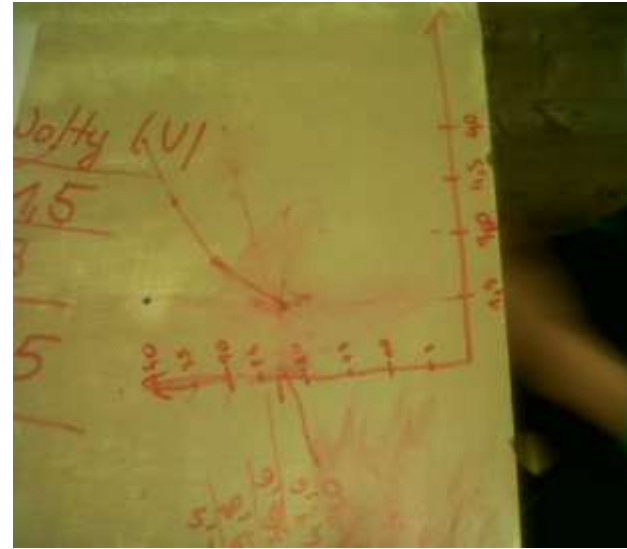
and what's next ?



Why? – why not :-)



but sometimes ...



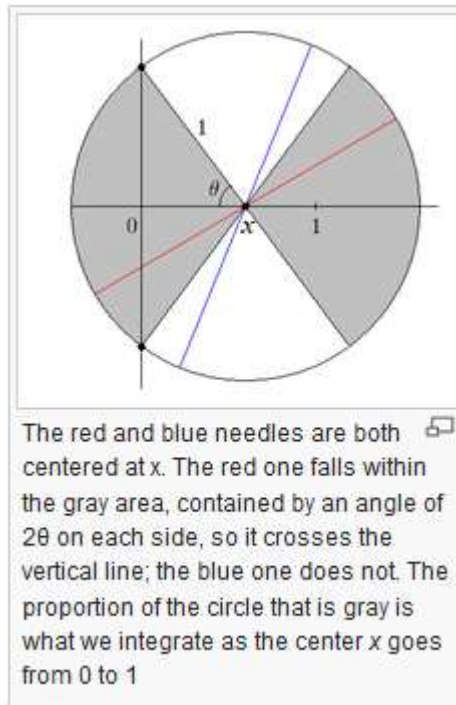
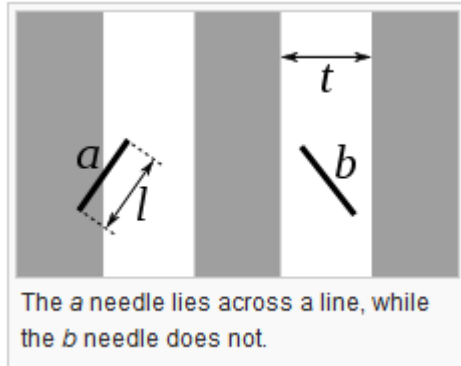
hope



Inquiry-based learning on maths?

Georges-Louis Leclerc, Comte de Buffon's problem was the inspiration to find the number π . It can be solved using integral geometry. Experiment cover topics of probability, geometry, Monte Carlo method and good fun :-)
Entertainment has become a good point to work on finding π with IBL





$$P = \frac{\int_0^{\frac{\pi}{2}} l \cos \theta d\theta}{\int_0^{\frac{\pi}{2}} t d\theta} = \frac{l \int_0^{\frac{\pi}{2}} \cos \theta d\theta}{\int_0^{\frac{\pi}{2}} d\theta} = \frac{l \cdot 1}{t \cdot \frac{\pi}{2}} = \frac{2l}{t\pi}, \text{ as above.}$$

In the first, simpler case above, the formula obtained for the probability P can be rearranged to: $\pi = \frac{2l}{tP}$. Thus, if we conduct an experiment to estimate P , we will also have an estimate for π .

Suppose we drop n needles and find that h of those needles are crossing lines, so P is approximated by the fraction h/n . This leads to the formula:

$$\pi \approx \frac{2l \cdot n}{th}$$





Exploring the Internet



$$\pi \approx \frac{2l \cdot n}{th}$$

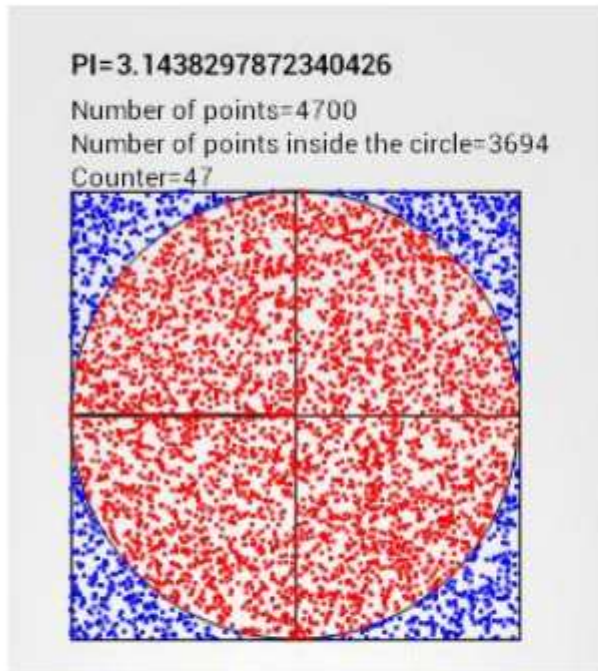
a ~~needle~~ of length l
shoe

t - the width of the line
 n - number of crossing lines

Pi determined from
photos

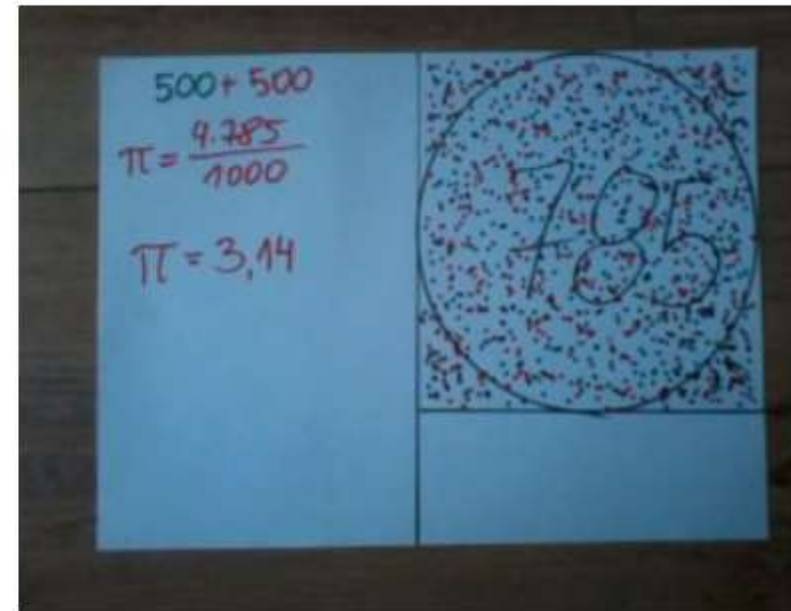
π = 16/5 = 3,2 😊

... and more..



phone print screen

vs.



studens job

...simplification...

$$\frac{P_{kola}}{P_{kwadrat}} = \frac{\pi r^2}{4r^2} = \frac{\pi}{4}$$



np. $m = 10g$

$\frac{P_o}{P_k} = \frac{\pi r^2}{4r^2} = \frac{\pi}{4}$

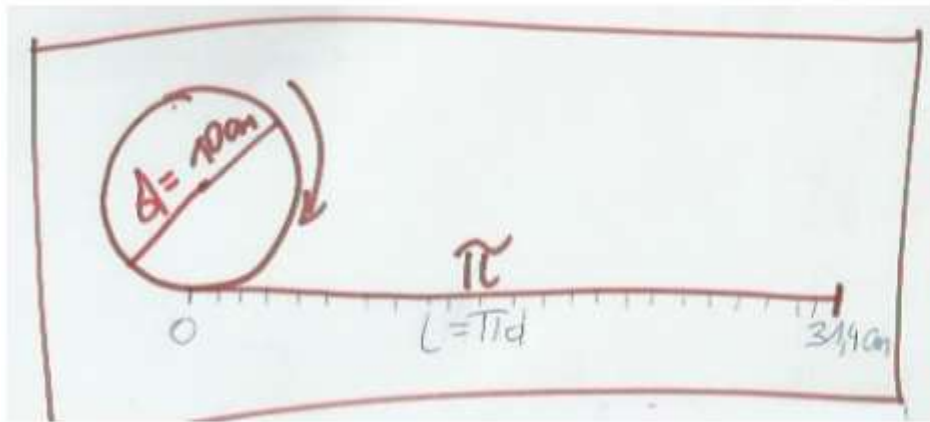
$\pi = \frac{4m_o}{m_k}$ (przy jednolitej grubości??)

$m = 12,3g$

NATOMIAST dla $m_o = 2,5g$
maso \square będzie równa π

$3,14g$

...and more simple...



blueprint



final product

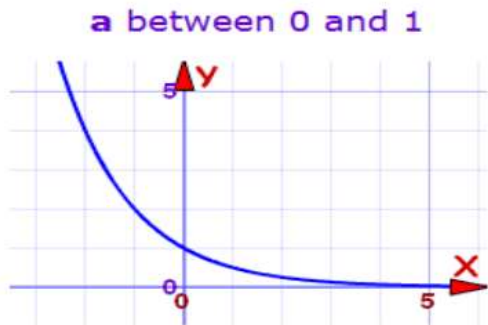
Make things as simple as possible, but not simpler

last measurements of pi



Future ??

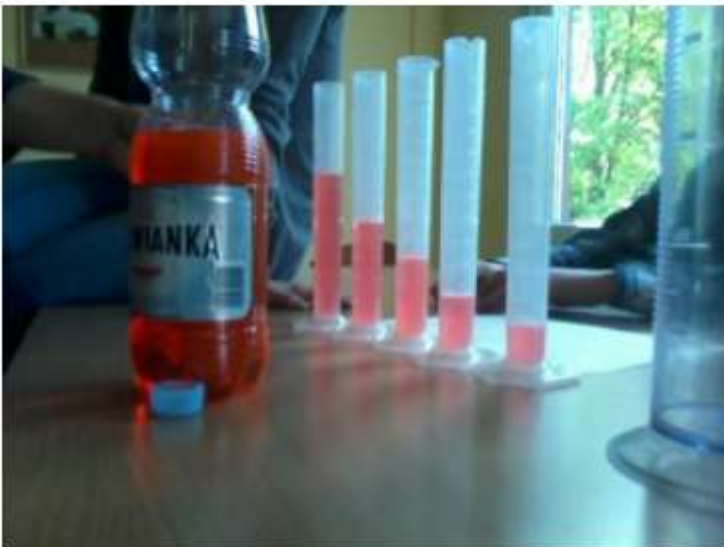
Experiment helps find a exponential function.



Example: $f(x) = (0,5)^x$



Each vessel is then filled half of the remaining water

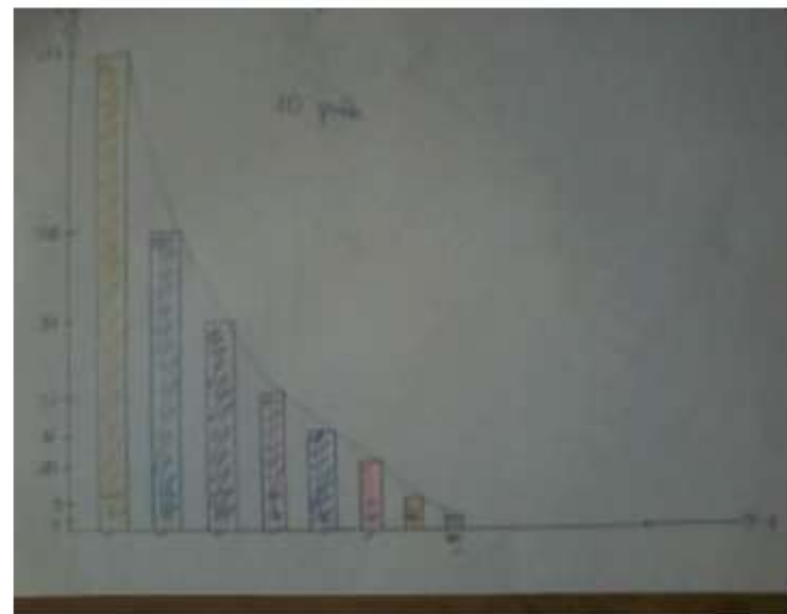


Effect of ten retries





Brainstorming

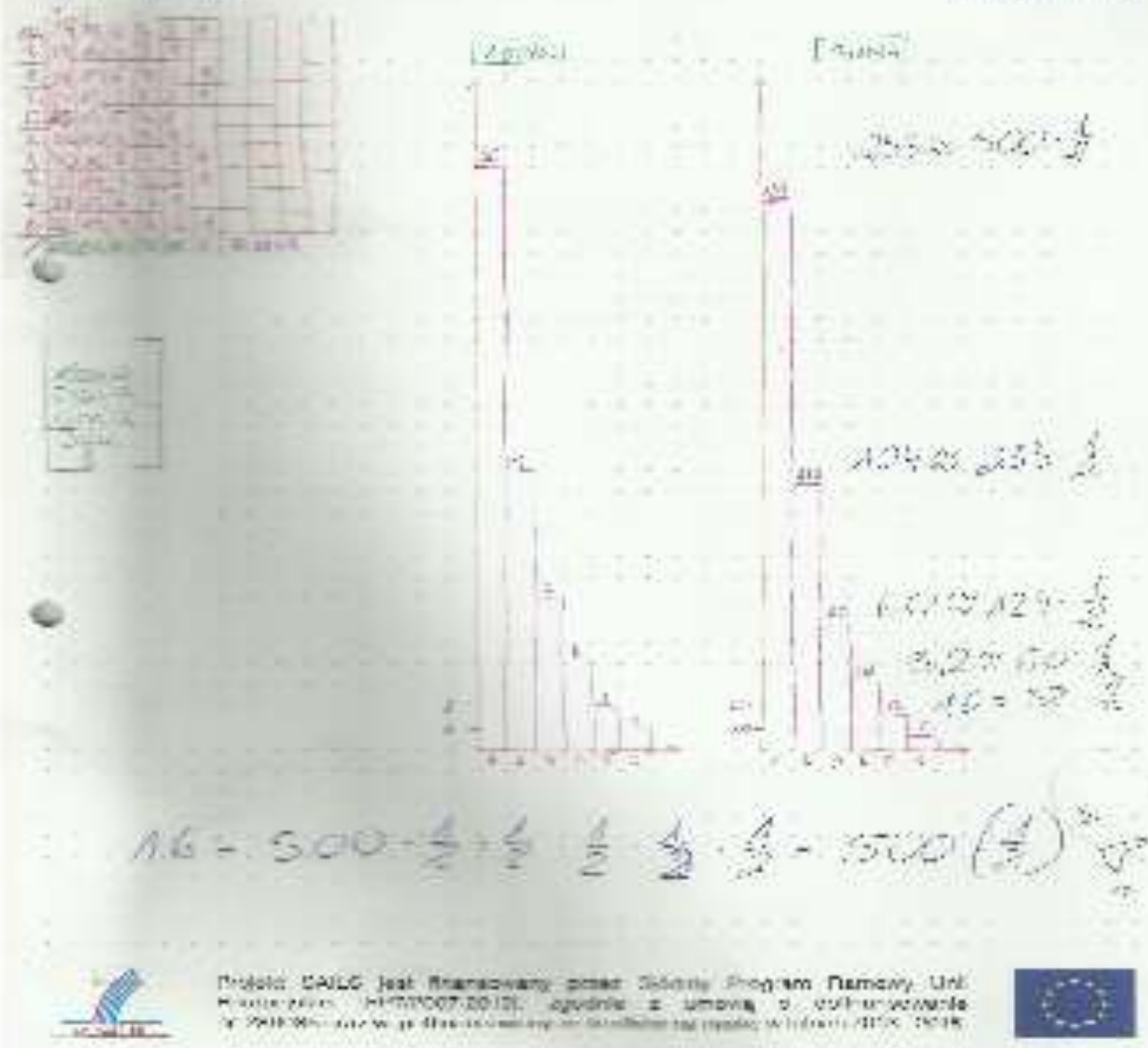


Experimentally obtained exponential function



SAILS Strategies for Assessment of Inquiry Learning in Science

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It's work !!!

Thanks a lot ...



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